

# Data Driven Modeling for Critical State Estimation in Power Grids

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## Introduction

- Power system state estimation critical to ensure smooth grid operations
- **State estimation:**  $z = Hx + e$
- **Data Injection Attacks:** spoof meter readings with  $a = Hc$ , so that error is undetected
- **LMP:** Locational Marginal Price
- **Problem Statement:** Given  $N$  buses, identify  $k \ll N$  buses which can determine the system state (as represented by LMPs) accurately

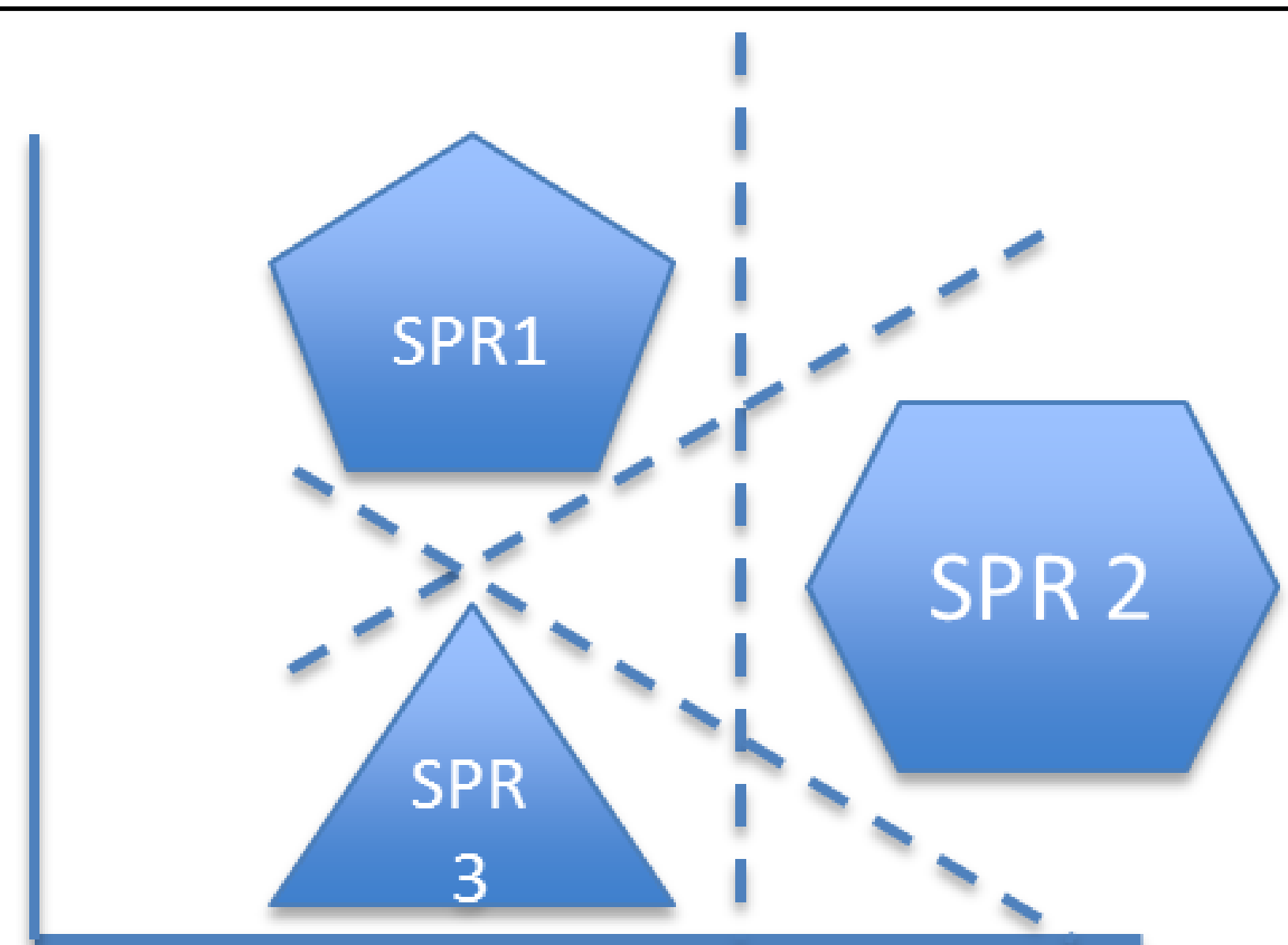
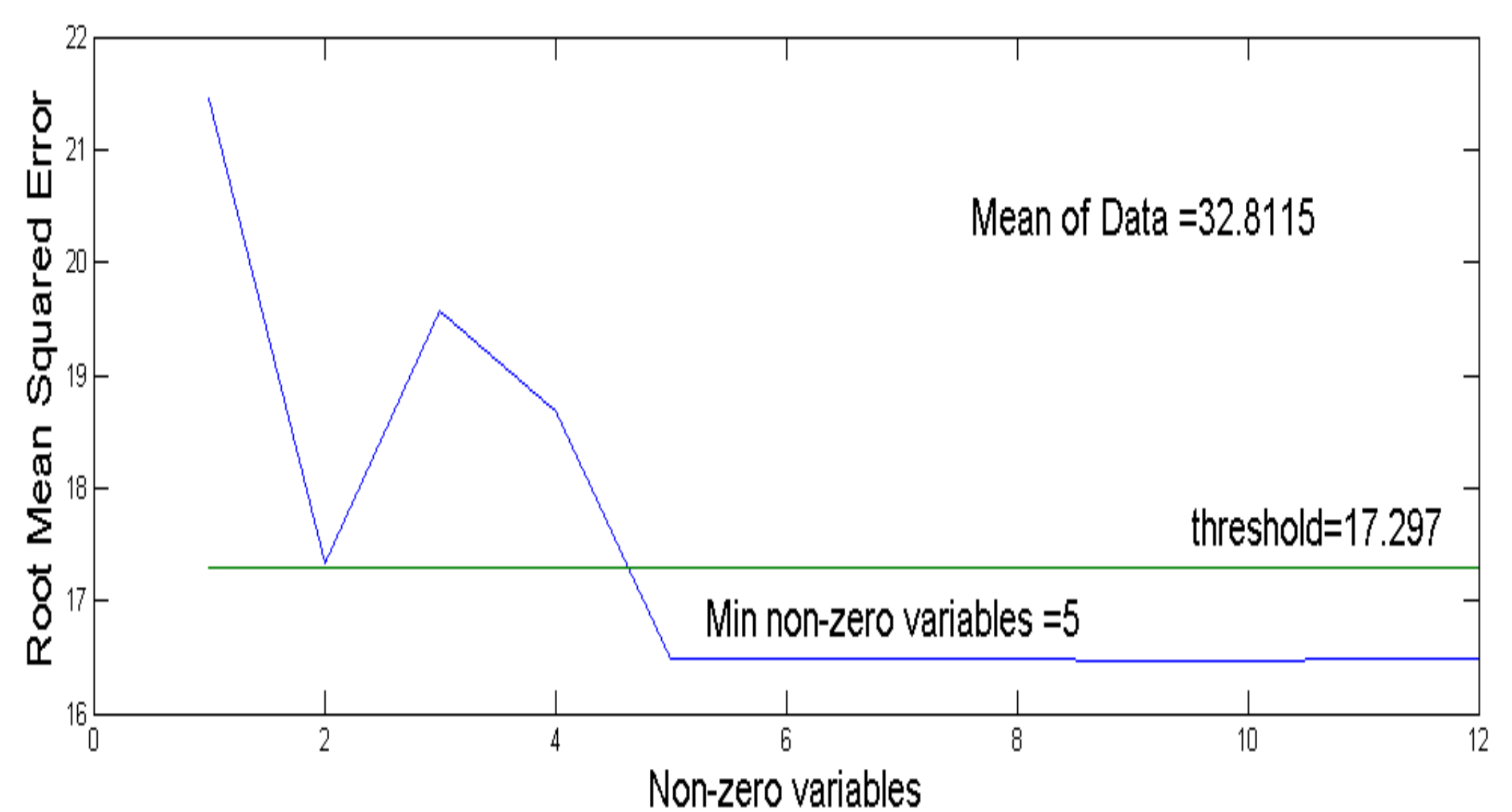
## Exploiting Power Flow Structure

- **System Pattern Region:** Range of load-vectors for which same  $N$  equations become tight
- **Theorem:** Load pattern space can be partitioned into **disjoint convex sets** each of which correspond to a unique system pattern region
- Approach (linear cost function):
  - Preprocess historical data and identify  $l$  most frequent system patterns (using LMPs)
  - Generate  $\frac{l(l-1)}{2}$  one-to-one SVM models
  - Use PCA on the  $R^{\wedge}\{\frac{l(l-1)}{2} \times n\}$  weight matrix to identify the minimum number of states which account for maximum variance (to meet threshold criteria)

## Lasso Regression

$$\min \left( \frac{1}{2m} \sum_{i=1}^m (y_i - \beta_0 - x_i^T \beta)^2 + \lambda \sum_{j=1}^n \beta_j \right)$$

- **Inputs:**  $x$ : load vector,  $y$ : price
- **Outputs:**  $\beta$  weights for each bus
- **Results:**
  - Lasso with 10 fold validation
  - Just 4-5 buses ensure <5% deviation from 14 bus error rate
- **Limitations:** Low accuracy



## Future Work

- Generalize for quadratic cost functions
- Challenge: LMP not unique for a region